

CHANGES TO DMA TR 8350.2-B,

SUPPLEMENT TO DEPARTMENT OF DEFENSE WORLD GEODETIC SYSTEM 1984 TECHNICAL
REPORT, PART II - PARAMETERS, FORMULAS, AND GRAPHICS FOR THE PRACTICAL
APPLICATION OF WGS 84, 1 December 1987.

The enclosed pages are changes as of 1 March 1989 which update both the first and second printings of the report.

Table 20.16

Local Geodetic System-to-MGS 84
Datum Transformation Multiple Regression Equations ($\Delta\phi$, $\Delta\lambda$, ΔH)
- ED 50 (Cyprus) to MGS 84 -

$$\begin{aligned}\Delta\phi'' &= - 3.84288 + 0.09188 U + 0.03581 V - 0.07481 UV \\ \Delta\lambda'' &= - 1.10294 - 0.04240 U + 0.12748 V - 0.32783 UV^2 + 0.51023 UV^3 - 0.01600 V^7 - 0.1718 U^3V^9 \\ \Delta H_m &= 24.430 - 5.719 U + 0.778 V + 5.631 U^2 - 23.892 UV + 18.980 U^2V - 0.988 V^3 + 106.027 U^3V \\ &\quad - 42.824 U^4V - 323.655 U^9V^2 + 2.261 U^4V^9\end{aligned}$$

In the preceding equations:

$$\begin{aligned}U &= K (\phi - 35) \\ V &= K (\lambda - 33) \\ K &= 0.78539816\end{aligned}$$

ϕ = geodetic latitude, local geodetic system, in degrees and decimal part of a degree;
positive north (0° to 90°), negative south (0° to -90°)
 λ = geodetic longitude, local geodetic system, in degrees and decimal part of a degree;
positive east from 0° to 360°

The preceding equations reproduced Doppler-derived MGS 84 geodetic coordinates at 16 comparison points to the following root-mean-square (RMS) differences:

$$\phi: \pm 0.5 \text{ m}; \quad \lambda: \pm 0.3 \text{ m}; \quad H \text{ (geodetic height): } \pm 0.2 \text{ m}$$

Test Case:

Input data for ED 50			
(Cyprus) test point:	$\phi =$	$34^\circ 43' 23.316'' \text{N}$	$\Delta\phi = -3.885''$
	$\lambda =$	$32^\circ 28' 06.026'' \text{E}$	$\Delta\lambda = -1.126''$
			$\Delta H = 23.64 \text{ m}$

Table 20.29

Local Geodetic System-to-WGS 84
Datum Transformation Multiple Regression Equations ($\Delta\phi$, $\Delta\lambda$, ΔH)
- Minna Datum* to WGS 84 -

$$\begin{aligned} \Delta\phi'' &= 0.49461 - 0.69094 U + 0.39940 V - 7.44709 U^3 - 1.82129 U^2V - 2.92752 UV^2 + 5.70789 U^3V \\ &\quad - 2.10838 U^2V^2 - 6.88780 UV^3 + 14.35602 U^5 + 5.10389 UV^4 + 6.18524 U^6 + 8.62320 UV^5 \\ &\quad + 48.52705 U^7V^2 - 0.49769 V^9 - 11.39331 U^4V^8 \\ \Delta\lambda'' &= -2.62435 - 0.21876 U + 0.43678 V + 0.35068 UV - 1.53864 U^2V - 0.46268 UV^3 + 2.20240 U^4V \\ &\quad - 0.11456 V^5 + 1.59485 U^3V^4 \\ \Delta H_m &= 20.013 + 2.098 U - 11.691 V + 47.983 U^2V - 60.195 U^4V - 21.214 U^2V^3 + 8.642 V^5 - 12.588 U^5V \\ &\quad - 27.760 U^3V^8 \end{aligned}$$

In the preceding equations:

$$U = K (\phi - 10)$$

$$V = K (\lambda - 8)$$

$$K = 0.15707963$$

ϕ = geodetic latitude, local geodetic system, in degrees and decimal part of a degree; positive north (0° to 90°), negative south (0° to -90°)

λ = geodetic longitude, local geodetic system, in degrees and decimal part of a degree; positive east from 0° to 360°

The preceding equations reproduced Doppler-derived WGS 84 geodetic coordinates at 23 comparison points to the following root-mean-square (RMS) differences:

<u>Test Case:</u>	ϕ : ± 1.2 m;	λ : ± 1.0 m;	H (geodetic height): ± 0.7 m
Input data for Minna	$\phi =$	$9^\circ 19' 09.051'' N$	$\Delta\phi = 0.930''$
Datum test point:	$\lambda =$	$12^\circ 13' 50.125'' E$	$\Delta\lambda = -2.348''$
			$\Delta H = 13.43 m$

* Nigeria

Table 20.31

Local Geodetic System-to-WGS 84
Datum Transformation Multiple Regression Equations ($\Delta\phi$, $\Delta\lambda$, ΔH)
- NAD 27 (Alaska) to WGS 84 -

$$\begin{aligned} \Delta\phi'' = & - 2.08611 + 0.59833 U + 0.52967 V + 0.23473 U^2 + 0.23563 UV + 0.28672 UV^2 + 0.27573 V^3 \\ & + 0.19561 U^4 - 0.15184 U^3V - 0.21241 U^2V^2 + 0.04891 V^4 - 0.18860 UV^4 - 0.17032 V^5 - 0.05741 UV^5 \\ & - 0.04292 U^2V^5 + 0.02097 V^7 - 0.01487 U^2V^6 - 0.00384 V^8 - 0.18402 U^9 - 0.00188 U^3V^7 \\ \Delta\lambda'' = & - 8.19369 - 1.56665 U + 0.73861 V - 3.10809 U^2 - 0.35323 UV - 0.06926 V^2 - 0.68114 UV^2 \\ & - 0.32398 V^3 + 0.74679 U^4 + 0.43200 U^3V + 4.24388 U^2V^2 + 0.14065 UV^3 - 0.30990 U^2V^3 \\ & + 0.11365 V^5 - 1.48566 U^4V^2 - 1.96501 U^2V^4 + 2.04229 U^6V - 0.48255 U^5V^2 + 0.09847 UV^6 \\ & + 0.49313 U^2V^6 - 1.00218 U^8V - 0.02809 U^2V^8 + 0.00054 U^5V^9 \\ \Delta H_m = & 8.352 - 13.742 U - 8.268 V + 0.900 V^2 + 5.340 U^3 + 2.960 UV^2 - 2.016 V^3 + 5.087 U^3V + 1.437 UV^3 \\ & + 0.951 V^5 - 2.461 U^3V^4 - 1.560 U^8 - 1.980 U^7V - 0.205 U^5V^3 + 0.094 UV^8 - 2.885 U^8V^2 \\ & - 0.011 UV^9 \end{aligned}$$

In the preceding equations:

$$\begin{aligned} U &= K (\phi - 62) \\ V &= K (\lambda - 208) \\ K &= 0.10471975 \end{aligned}$$

ϕ = geodetic latitude, local geodetic system, in degrees and decimal part of a degree;
positive north (0° to 90°), negative south (0° to -90°)
 λ = geodetic longitude, local geodetic system, in degrees and decimal part of a degree;
positive east from 0° to 360°

The preceding equations reproduced Doppler-derived WGS 84 geodetic coordinates at 85, 86, and 86 comparison points to the following root-mean-square (RMS) differences, respectively:

$$\phi: \pm 1.7 \text{ m}; \quad \lambda: \pm 1.7 \text{ m}; \quad H \text{ (geodetic height): } \pm 1.2 \text{ m}$$

Test Case:

Input data for NAD 27 (Alaska) test point:	$\phi = 64^\circ 31' 09.064'' \text{N}$	$\Delta\phi = -2.648''$
	$\lambda = 194^\circ 37' 28.092'' \text{E}$	$\Delta\lambda = -9.525''$
		$\Delta H = 19.20 \text{ m}$

Table 20.32

Local Geodetic System-to-WGS 84
Datum Transformation Multiple Regression Equations ($\Delta\phi$, $\Delta\lambda$, ΔH)
- NAD 27 (Canada) to WGS 84 -

$$\begin{aligned}
 \Delta\phi'' = & 0.79395 + 2.29199 U + 0.27589 V - 1.76644 U^2 + 0.47743 UV + 0.08421 V^2 - 6.03894 U^3 \\
 & - 3.55747 U^2V - 1.81118 UV^2 - 0.20307 V^3 + 7.75815 U^4 - 3.10170 U^3V + 3.58363 U^2V^2 \\
 & - 1.31086 UV^3 - 0.45916 V^4 + 14.27239 U^5 + 3.28815 U^4V + 1.35742 U^2V^3 + 1.75323 UV^4 \\
 & + 0.44999 V^5 - 19.02041 U^4V^2 - 1.01631 U^2V^4 + 1.47331 UV^5 + 0.15181 V^6 + 0.41614 U^2V^5 \\
 & - 0.80920 UV^6 - 0.18177 V^7 + 5.19854 U^4V^4 - 0.48837 UV^7 - 0.01473 V^8 - 2.26448 U^9 \\
 & - 0.46457 U^2V^7 + 0.11259 UV^8 + 0.02067 V^9 + 47.64961 U^8V^2 + 0.04828 UV^9 + 36.38963 U^9V^2 \\
 & + 0.06991 U^4V^7 + 0.08456 U^3V^8 + 0.09113 U^2V^9 + 5.93797 U^7V^5 - 2.36261 U^7V^6 + 0.095775 U^5V^8 \\
 \\
 \Delta\lambda'' = & - 1.36099 + 3.61796 V - 3.97703 U^2 + 3.09705 UV - 1.15866 V^2 - 13.28954 U^3 - 3.15795 U^2V \\
 & + 0.68405 UV^2 - 0.50303 V^3 - 8.81200 U^3V - 2.17587 U^2V^2 - 1.49513 UV^3 + 0.84700 V^4 \\
 & + 31.42448 U^5 - 14.67474 U^3V^2 + 0.65640 UV^4 + 17.55842 U^6 + 6.87058 U^4V^2 - 0.21565 V^6 \\
 & + 62.18139 U^5V^2 + 1.78687 U^3V^4 + 2.74517 U^2V^5 - 0.30085 UV^6 + 0.04600 V^7 + 63.52702 U^6V^2 \\
 & + 7.83682 U^5V^3 + 9.59444 U^3V^5 + 0.01480 V^8 + 10.51228 U^4V^5 - 1.42398 U^2V^7 - 0.00834 V^9 \\
 & + 5.23485 U^7V^3 - 3.18129 U^3V^7 + 8.45704 U^9V^2 - 2.29333 U^4V^7 + 0.14465 U^2V^9 + 0.29701 U^3V^9 \\
 & + 0.17655 U^4V^9 \\
 \\
 \Delta H_m = & - 26.806 + 9.266 U - 5.857 V + 14.794 U^2 + 3.497 UV + 9.600 V^2 - 7.664 UV^2 - 40.040 U^2V^2 \\
 & - 3.439 V^4 + 14.592 U^2V^3 - 23.902 U^5V + 15.246 U^4V^2 + 18.445 U^2V^4 + 0.770 V^6 - 130.424 U^6V \\
 & - 11.874 U^2V^5 - 100.769 U^7V - 3.165 U^2V^6 - 0.182 UV^7 - 0.066 V^8 + 2.404 U^2V^7 + 0.073 UV^8 \\
 & - 0.074 U^2V^9
 \end{aligned}$$

Table 20.41

Local Geodetic System-to-WGS 84
Datum Transformation Multiple Regression Equations ($\Delta\phi$, $\Delta\lambda$, ΔH)
- Qatar National Datum* to WGS 84 -

$$\begin{aligned}\Delta\phi'' &= 2.47363 + 0.08786 U + 0.14283 U^2 + 0.04380 UV + 0.07142 V^2 - 0.08879 UV^2 - 0.11089 U^5 \\ &\quad - 0.06321 U^3V^4 + 0.01669 U^9 \\ \Delta\lambda'' &= -2.80439 + 0.10489 V + 0.02697 V^2 - 1.10721 U^2V^2 + 2.88786 U^2V^3 - 0.06281 U^5V - 2.59921 U^3V^6 \\ \Delta H_m &= -28.376 + 2.381 U - 1.126 U^2 + 3.095 V^2 - 4.112 U^3V^3 - 13.156 V^7 - 2.048 U^8 + 1.618 U^9 \\ &\quad + 18.689 UV^8\end{aligned}$$

In the preceding equations:

$$\begin{aligned}U &= K (\phi - 25) \\ V &= K (\lambda - 51) \\ K &= 1.04719754\end{aligned}$$

ϕ = geodetic latitude, local geodetic system, in degrees and decimal part of a degree;
positive north (0° to 90°), negative south (0° to -90°)
 λ = geodetic longitude, local geodetic system, in degrees and decimal part of a degree;
positive east from 0° to 360°

The preceding equations reproduced Doppler-derived WGS 84 geodetic coordinates at 15 comparison points to the following root-mean-square (RMS) differences:

ϕ : ± 0.3 m; λ : ± 0.2 m; H (geodetic height): ± 0.2 m

Test Case:

Input data for Qatar National	$\phi =$	24°34'55.061"N	$\Delta\phi =$	2.465"
Datum test point:	$\lambda =$	50°59'06.940"E	$\Delta\lambda =$	-2.806"
			$\Delta H =$	-29.64 m

* Qatar Island (Persian Gulf)

Table 23.21

Multiple Regression Equation for DMA-Developed
Local Geodetic System Geoid Heights
- Kandawala Datum* -

$$N_m = - 0.979 + 1.853 U - 3.443 U^2 + 2.523 U^3 - 5.423 U^2V - 5.278 V^3 + 3.965 U^4V^3 - 0.899 U^7V^2 + 5.225 U^2V^9$$

In the preceding equation:

$$U = K (\phi - 7)$$

$$V = K (\lambda - 80)$$

$$K = 0.52359877$$

ϕ = geodetic latitude, local geodetic system, in degrees and decimal part of a degree; positive north (0° to 90°), negative south (0° to -90°)
 λ = geodetic longitude, local geodetic system, in degrees and decimal part of a degree; positive east from 0° to 360°
 N = DMA-developed Kandawala Datum geoid height (in meters) referenced to the Everest Ellipsoid

23
9
22

The preceding equation reproduced the geoid heights from which it was generated to a root-mean-square (RMS) difference of ± 0.4 meter; 17 sites involved in the comparison.

Test Case:

Input data for Kandawala Datum	$\phi = 7^{\circ}37'02.730''N$	$N = -4.55$ m (Everest Ellipsoid)
test point:	$\lambda = 81^{\circ}40'49.750''E$	

* Sri Lanka; Everest Ellipsoid

Table 23.27

Multiple Regression Equation for DMA-Developed
Local Geodetic System Geoid Heights
- Nahrwan Datum* -

$$N_m = 7.464 - 3.286 U - 3.024 V - 3.944 U^2 - 4.720 V^2 - 2.019 U^3 - 1.613 V^3$$

In the preceding equation:

$$U = K (\phi - 23)$$

$$V = K (\lambda - 57)$$

$$K = 0.41887902$$

ϕ = geodetic latitude, local geodetic system, in degrees and decimal part of a degree;
positive north (0° to 90°), negative south (0° to -90°)

λ = geodetic longitude, local geodetic system, in degrees and decimal part of a degree;
positive east from 0° to 360°

N = DMA-developed Nahrwan Datum geoid height (in meters) referenced to the Clarke 1880 Ellipsoid

The preceding equation reproduced the geoid heights from which it was generated to a root-mean-square (RMS) difference of ± 1.2 meters; 19 sites involved in the comparison.

Test Case:

Input data for Nahrwan $\phi = 24^\circ 58' 07.671'' N$ N = 1.11 m (Clarke 1880 Ellipsoid)
Datum test point: $\lambda = 55^\circ 00' 07.720'' E$

* Masirah Island (Oman) and United Arab Emirates only (Clarke 1880 Ellipsoid). Contact DMA (see PREFACE) if data in this form is needed for Saudi Arabia.